

# Mathematical Modelling of Health & Safety Related Flows – Future Direction

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- Where is modelling used?
- Real Life Scenarios
- Flows of Interest
- Evolution in Mathematical Modelling
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- Future

# Applications of Models

- Basic Research
- Consequence modelling to support
  - COMAH
  - Safety Cases
  - Land Use Planning applications
- Incident investigations
- Risk Assessments
  - Simplified Approaches
  - Quantified Risk Assessments (QRA)

# Examples : HSL

- Airflows through human airways
- Atmospheric dispersion modelling LNG dispersion / source terms
- Blast waves
- Fluid structure interaction (FSI)
- Gas leaks in enclosed spaces
- Gas dispersion in gas turbine enclosures
- Hydrogen Safety
- Natural ventilation on offshore platforms
- Smoke movement

# Real Life Scenarios – 1



Buncefield:  
Aerial photograph  
of the Buncefield  
incident



Buncefield:  
Northgate Building,  
located to the West  
of the HOSL site

# Real Life Scenarios – 2



**BLEVE: 2 ton  
LPG tank**



**Didcot Power Station:  
Turbine Hall**

# Real Life Scenarios – 3



Burner based on a Rolls Royce Tay can combustor, operating at  $P > 4.0$  MPa



High pressure jet of combustion products impacting on a flat plate (pre-test)

# Real Life Scenarios – 4



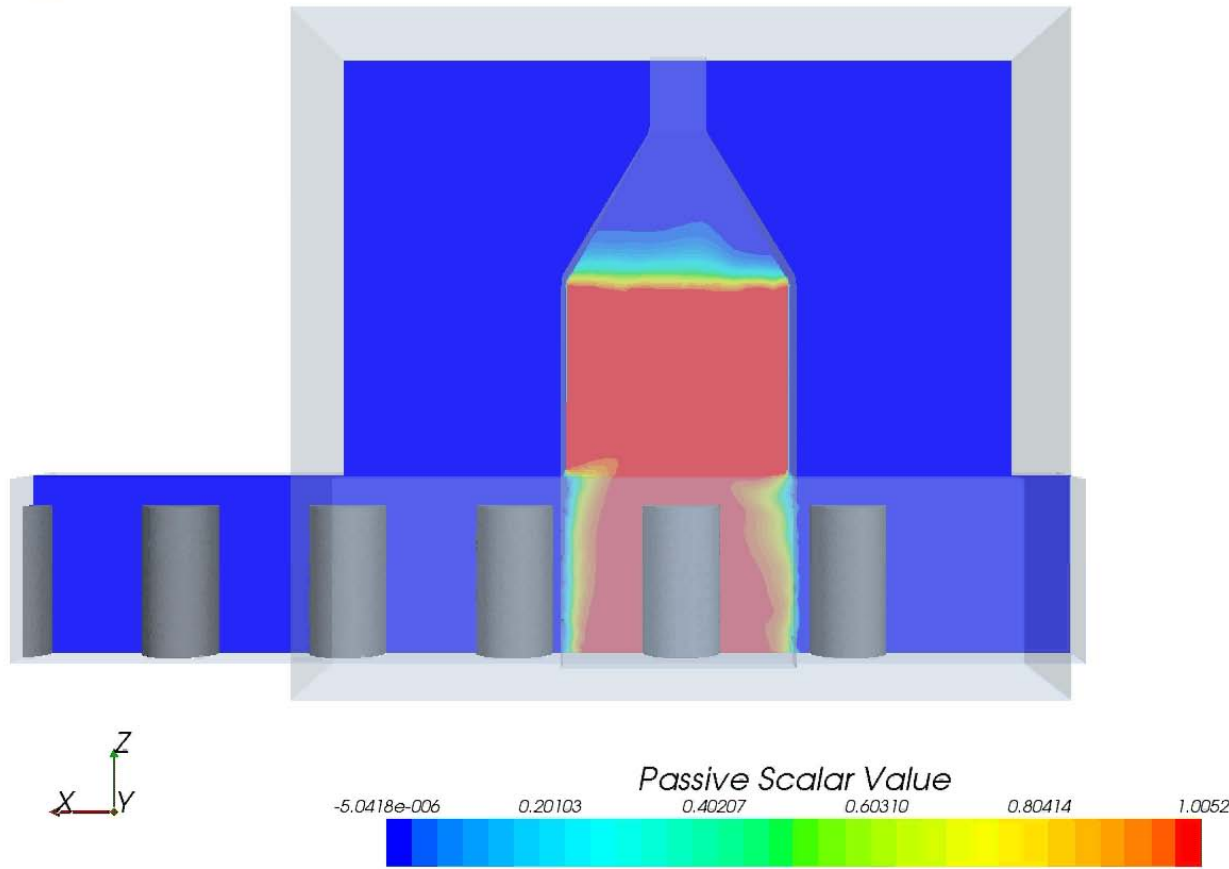
Family of offshore installations in the North Sea



Velocity measurements in one of the process modules. Note the congestion



# Drum Filling

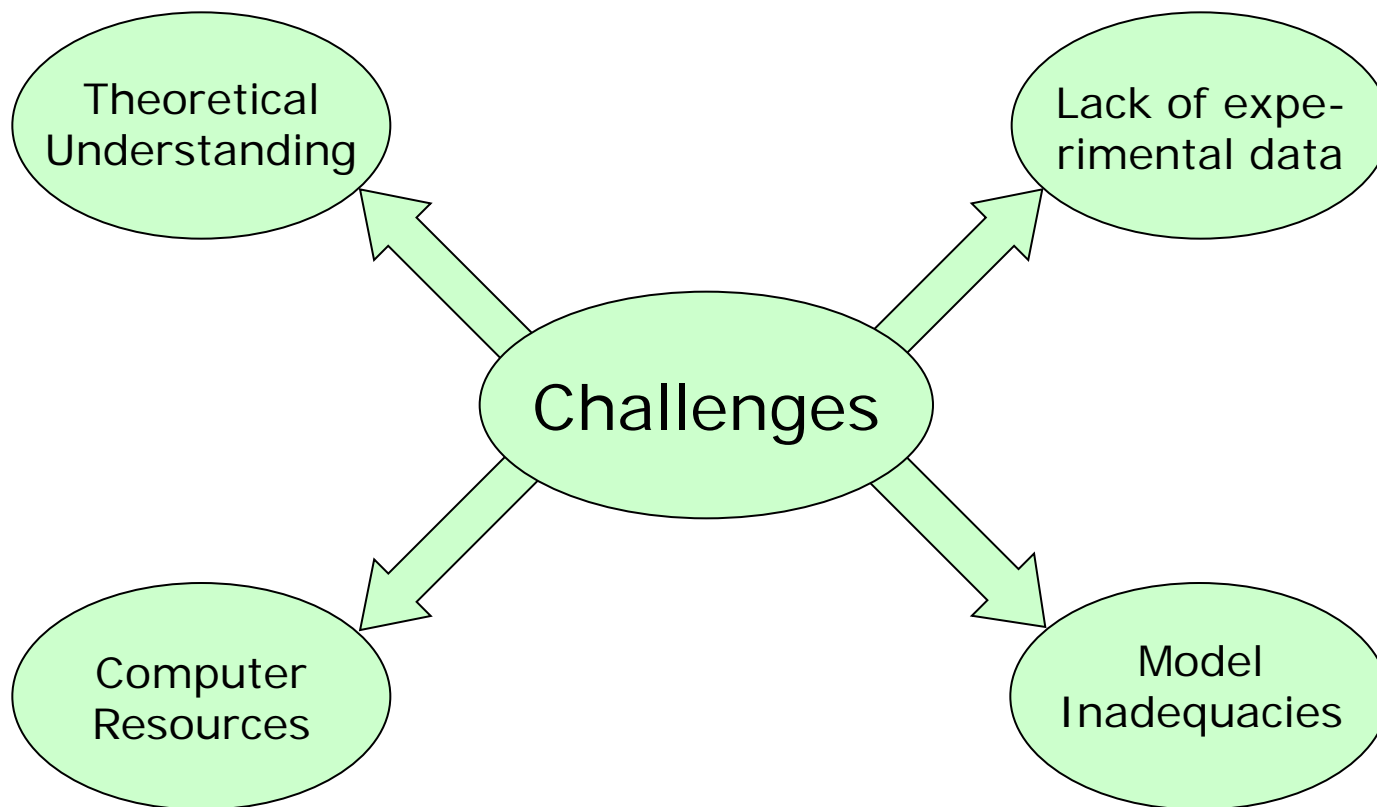


N.B. There are no experimental data available for this scenario.  
It is a proof-of-concept exercise

# Flows of Interest

- Dispersion
  - Biologically active substances
  - Flammable substances
  - Toxic substances
- Combustion
  - Deflagration
    - Explosions
    - Fires
  - Detonation, Deflagration to Detonation Transition (DDT)
  - Ignition
- Cryogenic liquids
- Supercritical fluids
- Free surface flows
- Free or impacting high-momentum jet
  - Combusting
  - Non-combusting
- Nano-particle laden flows
  - Occupational Health
  - Explosion
- Fluid-Structure Interaction
  - CFD and FEA
- Two-phase/multi-phase flows
- Phase transition

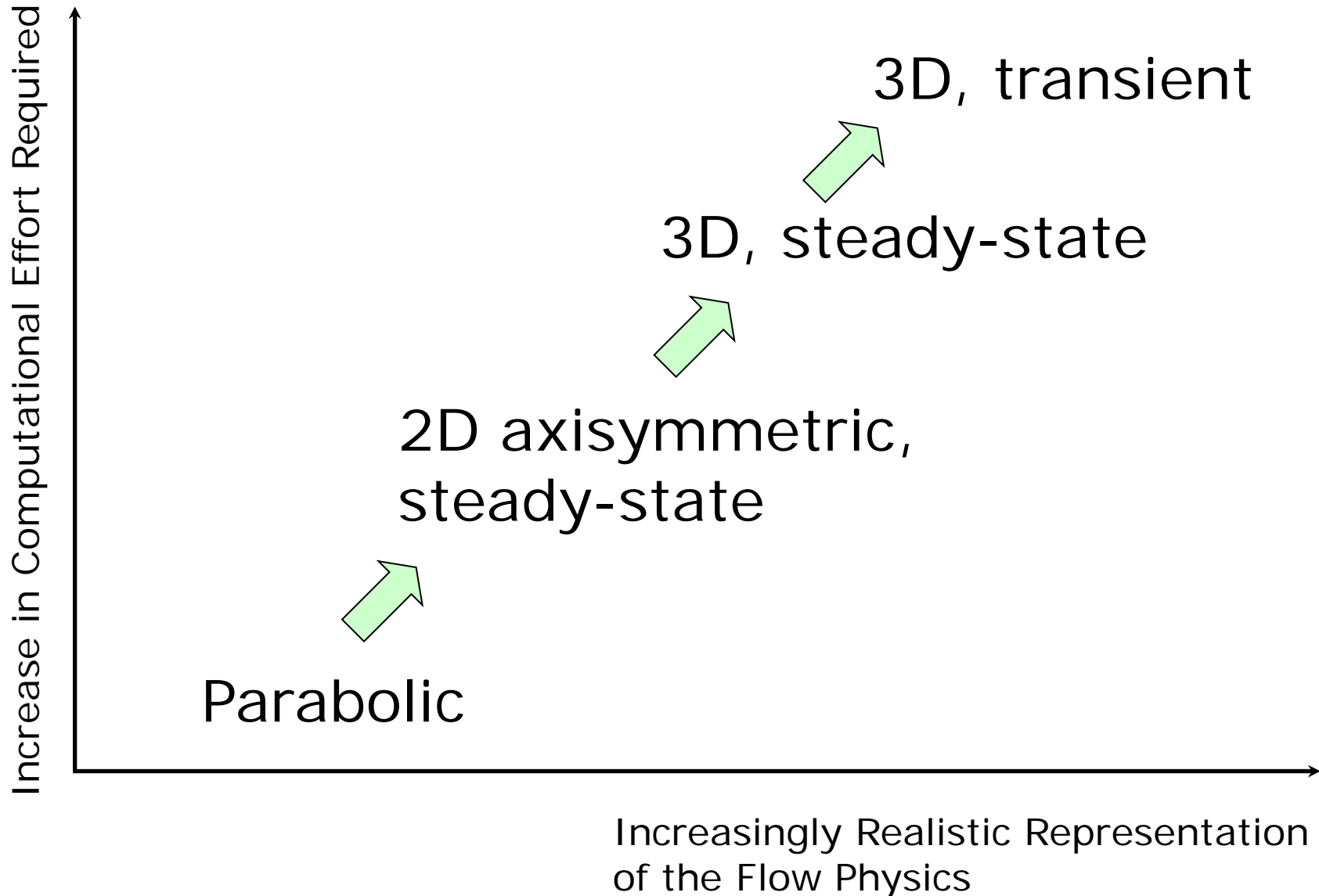
# Challenges – 1



# Challenges – 2

- DDT
- Deposition
- Deflagration
- Ignition
- Phase transition
- Two-phase and multi-phase flows
- And combinations of the above

# Progression



# Types of Models

- Empirical correlations – derived from a large number of experiments
- Simple models – may involve solving a set of ODEs for mass, momentum, etc.
- Statistical models
- CFD – realistic representation of the flow, but still broadly based on empirical data

Or Direct Numerical Simulation which means that all relevant length and time scales are resolved → No Modelling!!!

# Turbulence Modelling

- $k$ - $\varepsilon$  model
  - Launder, Spalding, Harlow, ... (1967-ish)
- $k$ - $\omega$ 
  - Wilcox (1985?)
  - Menter (1992)
- LES
  - Schumann (1975)
- RSTM
  - Hanjalic and Launder (1972, 1976)
  - Launder, Reece and Rodi (1975)

# Evolution – Turbulence (1)



- 1989
  - Two-equation Eddy Viscosity models
    - Variations on the  $k-\varepsilon$  model theme
    - Variations on the  $k-\omega$  model theme
  - Second moment closures (rarely)
    - Reynolds stress transport models
    - Algebraic Reynolds stress transport model
- 1999
  - Two-equation Eddy Viscosity models
    - Variations on the  $k-\varepsilon$  model theme
    - Variations on the  $k-\omega$  model theme
  - Second moment closures (rarely)
    - Reynolds stress transport models
    - Algebraic Reynolds stress transport model



# Evolution – Turbulence (2)



- 2009
  - Two-equation Eddy Viscosity models
    - Variations on the  $k-\varepsilon$  model theme
    - Variations on the  $k-\omega$  model theme
  - Large Eddy Simulations (LES)
    - Standard/Dynamic Sub-Grid Scale model
    - Detached Eddy Simulation (DES)
    - Scale Adaptive Simulation (SAS)
  - Second moment closures (very rarely)
    - Reynolds stress transport models
    - Algebraic Reynolds stress transport model

# Combustion Modelling – 1



- Eddy BreakUp model (P)
  - Spalding (1972)
- Eddy Dissipation Concept Model (NP)
  - Magnussen and Hjertager (1976)
- Laminar Flamelets – Non-Premixed
  - Bilger and others (late 1970s)
- Laminar Flamelets – Premixed
  - Moss, Bray and Libby and others (late 1970s)

Definitions – NP: Non-Premixed, P: Premixed, pP: Partially Premixed

# Combustion Modelling – 2



- Flame speed correlations (P)
  - Bradley and others (late 1970s)
- Transported PDF (Detailed/Reduced Chemical Kinetics) (NP)
  - Pope, Jones and Kollmann, and others (mid-1980s)
- Transported PDF (Detailed/Reduced Chemical Kinetics) (P)
  - Pope and others (late 1990s)

Definitions – NP: Non-Premixed, P: Premixed, pP: Partially Premixed

# Evolution – Combustion (1)



- 1989
  - Eddy Break-Up/Eddy Dissipation models (P/NP)
  - Laminar flamelets with prescribed PDF (P/PN)
  - Conditional Moment Closure (NP)
  - Reduced kinetics with transported PDF (NP)
- 1999
  - Eddy Break-Up/Eddy Dissipation models (P/NP)
  - Flame speed correlations (P)
  - Laminar flamelets with prescribed PDF (P/NP)
  - Conditional Moment Closure (NP)
  - Reduced kinetics with transported PDF (P/NP)

Definitions – NP: Non-Premixed, P: Premixed, pP: Partially Premixed

# Evolution – Combustion (2)



- 2009
  - Eddy Break-Up/Eddy Dissipation models (P/NP)
  - Flame speed correlations (P)
  - Zimont model (pP)
  - Detailed kinetics with transported PDF (P/NP)
  - Conditional Moment Closure [CMC] (NP)

The combustion models used in academia are usually more advanced than those used routinely in industry

Definitions – NP: Non-Premixed, P: Premixed, pP: Partially Premixed

# Evolution – Radiation (1)

- 1989
  - Optically thin / Optically thick assumption
  - P1
  - Four-flux and six-flux model
  - Discrete Ordinate model
  - Discrete Transfer model
- 1999
  - Optically thin / Optically thick assumption
  - P1
  - Four-flux and six-flux model
  - Discrete Ordinate model
  - Discrete Transfer model

# Evolution – Radiation (2)

- 2009
  - Discrete Ordinate model
  - Discrete Transfer model
  - Monte Carlo
  - Optically thin / Optically thick assumption
  - P1
  - Four-flux and six-flux model
  - With grey gas, mixed grey gas or narrow-band model

# Quality and Trust

- Verification
  - Models
    - Right equations
    - Right terms
  - Coding
- Validation
- Application of appropriate mathematical tools
  - Include all important physical processes
  - Right models
- Degree of uncertainty
  - Uncertainties in the input
  - Uncertainties in the modelling
- Best Practice Guidance
  - Generic
  - Application specific
- Training
  - Academic (MSc/PhD?)
  - Specific training on using the mathematical tools
- Proper documentation of the simulations
  - Assumptions
  - Parameter settings, mesh
- Sensitivity analysis
  - Mesh resolution
  - Time step
  - Ray/photon dependence



# Future Direction – 1

- Turbulence models
  - Two-equation turbulence models, such as the  $k-\omega$  and the  $k-\varepsilon$  models will find continued extensive use
  - LES/DES/SAS will become more widely used, especially for fire modelling
  - Reynolds stress models (and algebraic Reynolds stress models) may be used to model specific scenarios
- Combustion models
  - Eddy Break-Up model and Eddy Dissipation Concept models will still be used
  - Laminar flamelets with prescribed or transported PDF are unlikely to replace EBU/EDC models
  - Detailed/Reduced kinetics with transported PDF
  - CMC – interesting for non-premixed combustion, but not making great inroads as yet

# Future Direction – 2



- Radiation models
  - Discrete Transfer Model and Discrete Ordinate Model are sufficiently sophisticated in many situations
  - Monte Carlo method is applicable to all scenarios

# Issues to Consider

- Characterisation of the source term
- Parameter values
- Boundary conditions
- Representing atmospheric conditions
  - Stable
  - Unstable
- Long transient simulations
- Experimental data
  - Lack of data
  - Uncertainty re. what was actually measured
  - Ambient and initial conditions

# Other Remedies – 1

- Moore's Law – doubling of the number of transistors on a microchip every 2 years
  - Constraints by physics
  - Manufacture of chips more difficult
  - Cooling issues
  - Current projections are that Moore's Law will apply for another decade
- Parallel processing
  - Improved chip architecture
  - Better algorithms

# Other Remedies – 2



- Adaptive Mesh Refinement and De-refinement

# Thank You for your attention!

## Any Questions?